

# Information retrieval

Evaluation of retrieval systems and learn to rank

Clovis Galiez

Laboratoire Jean Kuntzmann, Statistiques pour les sciences du Vivant et de l'Homme

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# Objectives of the course

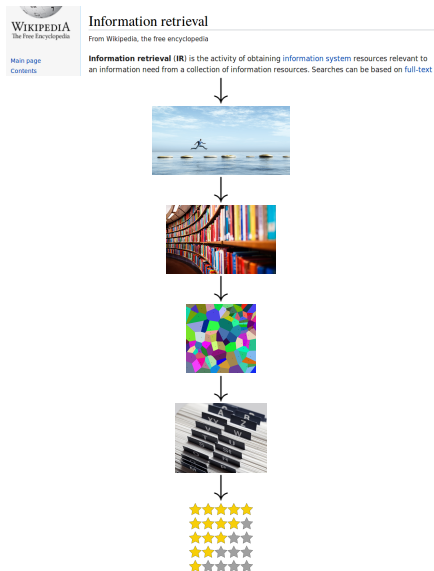
- Acquire a culture in information retrieval
- Master the basics concepts allowing to understand:
  - what is at stake in novel IR methods
  - what are the technical limits

This will allow you to have the basics tools to analyze current limitations or lacks, and imagine novel solutions.

# What's coming ahead (outline)

- Summary of last lectures
- Machine learning in IR:
  - Embeddings
  - Evaluation of IR systems
  - Learning to search
- Hands-on: complete your project!

# IR main steps



# The tf-idf matrix

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## Definition

The matrix  $M$  which rows – corresponding to each document – are:

$$D_t = \frac{\# \text{ t in D}}{\# \text{ tokens in D}} \times I(t)$$

is called the **tf-idf** (term frequency-inverse document frequency) representation.

## Question

What are the advantages of the vector model ?

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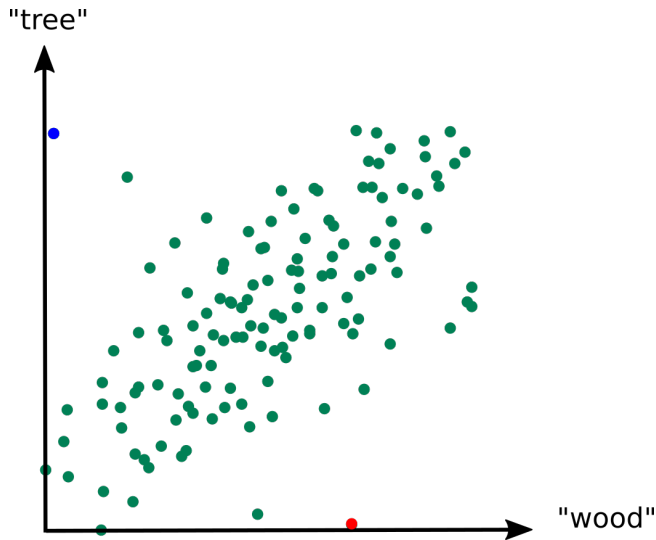
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## Question

What are the advantages of the vector model ?

- Have a direct weighting by information carried by tokens
- Framework for latent semantics

# Exploiting token correlation in documents





# Latent semantics: low rank approximation

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## Theorem

Let  $M$  be the tf matrix:  $M_{ij}$  is the frequency of token  $j$  in document  $i$ .  $M^\top M$  is symmetric and its eigenvectors are orthogonal and form a basis of the token space.

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What NLP issue does the IR latent semantics tackle?

# PageRank

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What PageRank is good for?  
What data is used as input?  
How does it work?

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What data is used as input?

How does it work?

**Data:**  $A :=$  graph of the WWW  $A_{ij} = \begin{cases} \frac{1}{N_j} & \text{if link from } j \text{ to } i \\ 0 & \text{else} \end{cases}$

**Result:** Ranking of web pages

$R_0 := S$  ;

**repeat**

$R^{(i+1)} \leftarrow AR^{(i)}$   
     $\delta \leftarrow ||R^{(i)} - R^{(i+1)}||_1$

**until**  $\delta \leq \epsilon$ ;

**Algorithm 2:** simplified PageRank

# Machine learning in IR

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Recent techniques (well, mostly since 2013)

Machine learning techniques can be used to **learn better vector representation<sup>a</sup> of tokens**, and more generally of any data (document, sentence, word, image, etc.).

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<sup>a</sup>aka embeddings

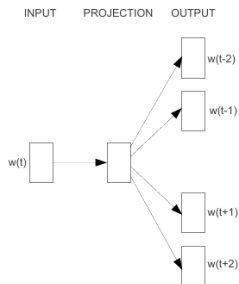
# Embeddings: a general technique with many derivatives

Many models have been developed for representing various type of data. Here is a small list of freely available models:

Model	Data represented
word2vec	Tokens
GloVe	Tokens
fastText	Tokens
doc2vec	Documents
dna2vec	Genomic sequences

## Word2vec: predict the context of a token

The core idea of word2vec is to learn a vector representation allows to predict the context of the token. Thereby, tokens appearing in similar context will be encoded closely in the vector space.



**Skip-gram**

[Mikolov, Tomas; et al. (2013)]

## word2vec's latent semantics

The word2vec embeddings have interesting semantic features<sup>1</sup>.

Table 8: *Examples of the word pair relationships, using the best word vectors from Table 4 (Skip-gram model trained on 783M words with 300 dimensionality).*

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

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<sup>1</sup>Note that GloVe is better at this



# Machine learning and IR performance evaluations

# Evaluation of IR systems



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For measuring relevance (ordered outcome): **Collection of documents** ranked by relevance associated to a query.

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## What gold standard?

It depends... For measuring correctness (binary outcome): **Collection of documents** associated to a query.

For measuring relevance (ordered outcome): **Collection of documents** ranked by relevance associated to a query.

Can be seen as a partial function  $g : \mathcal{Q} \times \mathcal{D} \rightarrow \mathbb{R}$  associating to a couple query-document its quantification of *correctness*, *relevance* or *truth*.

## Indicators for binary gold standards<sup>2</sup>

Special case:  $\text{dom}(g) = \{0, 1\}$ .

### Question

What is a False Positive? True Negative?

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Document ( $d$ )	rank	$g(q,d)$
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laposte.fr	0.01	0
election.gov.us/results	0.9	1
mediapart.fr/America	0.7	1

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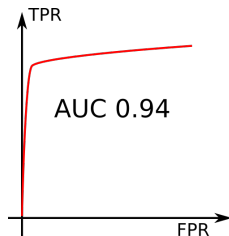
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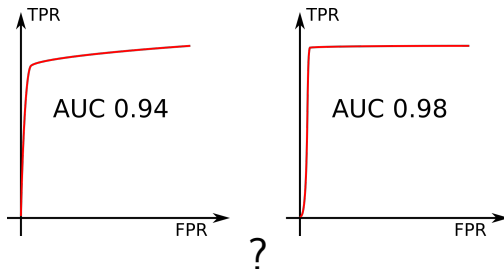
$$TPR_{\tau} = \frac{TP_{\tau}}{P}, FPR_{\tau} = \frac{FP_{\tau}}{N}$$

<sup>2</sup>To be used for assessing correctness for instance.

# Beware of summary indicators!



Use the right summary indicator (e.g. AUC-ROC/AUC-ROC5).



## Indicators for rank gold standards<sup>3</sup>

Ranking functions  $f_1, f_2 : \mathcal{Q} \times \mathcal{D} \rightarrow \mathbb{R}_+^*$  (the higher, the more relevant the doc to the query).

How can we say that  $f_1$  is better than  $f_2$ ?

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## Indicators for rank gold standards<sup>3</sup>

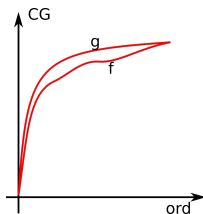
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How can we say that  $f_1$  is better than  $f_2$ ?

Given a gold standard  $g : \mathcal{Q} \times \mathcal{D} \rightarrow \mathbb{R}_+^*$ , we define the cumulative gain:

$$\text{CG}_n(q, f) = \sum_{k: \text{ord}_n(q, f)} g(q, k)$$

where  $\text{ord}_n(q, f)$  are the  $n$  first elements of  $\mathcal{D}$  when sorting by  $f(q, -)$ .



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## Indicators for ranking, stressing first results

In the same spirit of the difference AUC/AUC5, one can stress more the first results, by weighting the relevance by a *discount*<sup>4</sup> function:

$$\text{DCG}(q, f) = \sum_{k: \text{ord}_{N_Q}(q, f)} \frac{g(q, k)}{\log(k+1)}$$

where  $N_Q$  is  $\text{card}\{d | (q, d) \in \text{dom}(g)\}$  and  $i$  is the index in the summation.

The normalized DCG is defined as:

$$\text{NDCG}(q, f) = \frac{\text{DCG}_{N_Q}(q, f)}{\text{DCG}_{N_Q}(q, g)}$$

---

<sup>4</sup>One can choose different discount functions, but  $\frac{1}{\log k}$  has nice theoretical foundations [Wang et al. JMLR 13] and is good in practice.

# Comparing ranking strategies

Ranking functions  $f_1, f_2 : \mathcal{Q} \times \mathcal{D} \rightarrow \mathbb{R}_+^*$ . How can we say that  $f_1$  is better than  $f_2$ ?

Can use the expected  $\text{NDCG}(q, f_i)$  summary statistic:

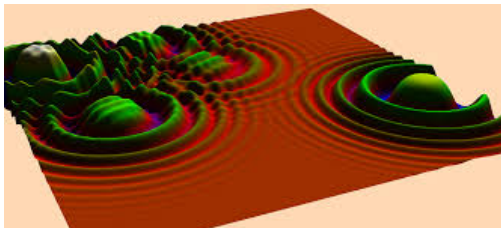
$$\rho_i = \frac{1}{Q} \sum_q \text{NDCG}(q, f_i)$$



As usual, averaging can hide bad performance when the gold standard is dominated by high performance on many similar queries.

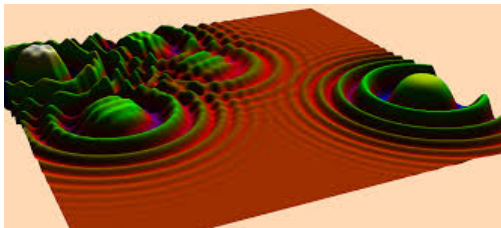
# Learning the parameters

Having a gold standard not only allows evaluation, but also optimization of the parameters.



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What parameters are we talking about?

## Some parameters to tune

At the semantics level:

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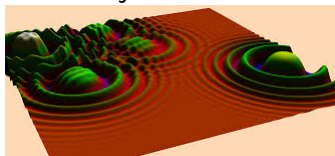
But also...

...the **trade-off** between the semantic scores (e.g. tf-idf vector model, text importance score) and the authority ranking score.



# Optimize the objective function by tuning the parameters

$$\text{obj} : \mathbb{R}^p \rightarrow \mathbb{R}$$



This is an optimization problem:

$$\arg \max_{\mathbb{R}^p} \text{obj}$$

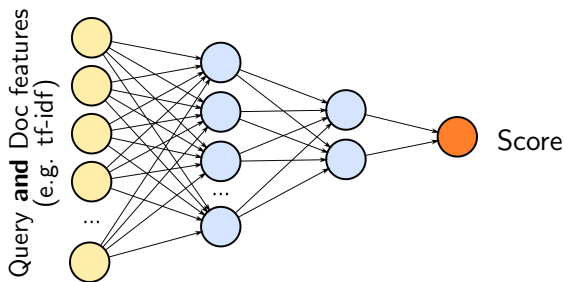
One can therefore use optimization strategies to maximize performance indicators by tuning  $p$  parameters.

# Why not going further?

Why learning only few parameters?

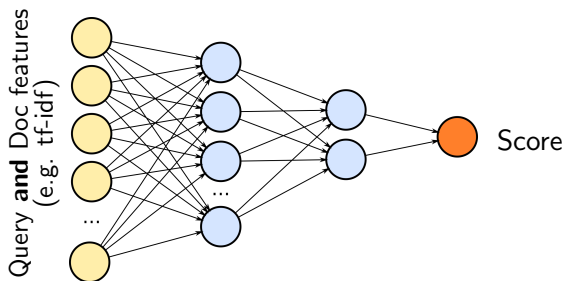
## Why not going further?

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## Issue

Curse of dimensionality, training set limitation, overtraining.

Ways out?

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- Reducing the dimensionality (embeddings, latent semantics)



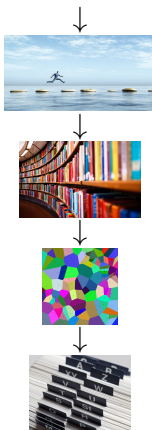
# Wrap-up I



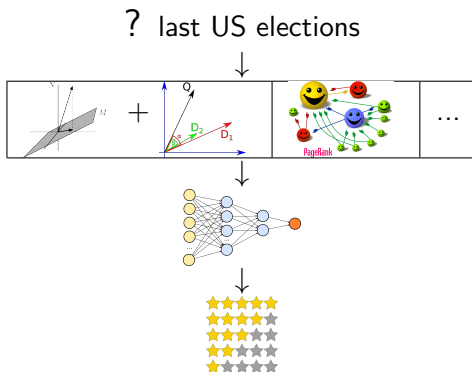
## Information retrieval

From Wikipedia, the free encyclopedia

**Information retrieval (IR)** is the activity of obtaining [information system](#) resources relevant to an information need from a collection of information resources. Searches can be based on [full-text](#)



## Wrap-up II



# Hope you enjoyed.

Find the material on <http://clovisg.github.io>

# Extras